Stat 470/670 Lecture 1

## What is Exploratory Data Analysis?

John W. Tukey

## EXPLORATORY DATA ANALYSIS



We will be exploring numbers. We need to handle them easily and look at them effectively. Techniques for handling and looking - whether graphical, arithmetic, or intermediate - will be important.

Tukey, Exploratory Data Analysis (1977)

A first example: Heights of the highest points by state

```
## load required packages and data
library(tidyverse)
options(tibble.print_min = 15)
heights = read_csv("highest-points-by-state.csv")
```

\#\# Rows: 50 Columns: 2
\#\# -- Column specification
\#\# Delimiter: ","
\#\# chr (1): state
\#\# dbl (1): elevation
\#\#
\#\# i Use ‘spec()` to retrieve the full column specification for this
data.
\#\# i Specify the column types or set 'show_col_types = FALSE' to quiet
this message.
\#\# switch from feet to meters
heights\$elevation = heights\$elevation * . 3048

A first try at looking at the data
heights


A second try at looking at the data

```
arrange(heights, elevation)
```



```
arrange(heights, desc(elevation))
```

| \#\# |  | elevation state |
| :---: | :---: | :---: |
| \#\# |  | <dbl> <chr> |
| \#\# | 1 | 6168. Alaska |
| \#\# | 2 | 4418. California |
| \#\# | 3 | 4399. Colorado |
| \#\# | 4 | 4392. Washington |
| \#\# | 5 | 4207. Wyoming |
| \#\# | 6 | 4205. Hawaii |
| \#\# | 7 | 4123. Utah |
| \#\# | 8 | 4011. New Mexico |
| \#\# | 9 | 4005. Nevada |
| \#\# | 10 | 3901. Montana |
| \#\# | 11 | 3859. Idaho |
| \#\# | 12 | 3851. Arizona |
| \#\# | 13 | 3426. Oregon |
| \#\# | 14 | 2667. Texas |
| \#\# | 15 | 2207. South Dakota |
|  |  | .. with 35 more rows |

Stem-and-leaf plots

Goals:

- Write down the set of numbers, keeping as much detail as possible
- Pack the numbers efficiently, so you can see all of them at once

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These are in conflict!

Stem-and-leaf plots

Remedy:

- Notice that parts of the numbers (the beginnings) are repeated.
- The first digit of each number is printed at the beginning of the line, the remainder at the ends.
- The first digit is the "stem", the remainder are the "leaves".

Stem-and-leaf-plot example

Set of numbers:
$16,17,17,17,17,18$
Stem-and-leaf display:
1 | 677778

Stem-and-leaf plot for the elevations in meters:

```
stem(heights$elevation)
```

```
##
## The decimal point is 3 digit(s) to the right of the |
##
## 0 | 11222445555667778
## 1 | 0011123355566779
## 2 | 0027
## 3 | 4999
## 4 | 00122444
## 5 |
## 6 | 2
```

The stem-and-leaf plot shows that there are three groups of states:

- Alaska
- The western and Rocky Mountain states (California, Colorado, Washington, Wyoming, Hawaii, Utah, New Mexico, Nevada, Montana, Idaho, Arizona, Oregon)
- All the other states

Note 1

## Hoosier Hill: Elevation 1257 feet



Source: google street view

Note 2

Compare the stem-and-leaf plot with a density estimate

```
ggplot(heights, aes(x = elevation)) + geom_density()
```



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```
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```



Where is Alaska?

Compare the stem-and-leaf plot with a density estimate

```
ggplot(heights, aes(x = elevation)) + geom_density() + geom_rug()
```



Where is Alaska?

We have made an advance in understanding this set of numbers!

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What would traditional statistics have to say about these numbers?

## What if we have a many more numbers, e.g. census data?

The Return for South Carolina having been made fince the foregoing Schedule was originally printed, the whole Enumeration is here given complete, except for the N . Weftern Territory, of which no Return has yet been publifhed.


Source: US Census Bureau Public Information Office, via the National Geographic Society

Or a large matrix?

| 5 | 5 | 8 | 0 | 3 | 4 | 9 | 9 | 5 | 3 | 6 | 4 | 3 | 5 | 6 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3 | 9 | 1 | 3 | 0 | 7 | 2 | 6 | 0 | 2 | 7 | 5 | 0 | 4 | 0 | 7 | 9 | 7 |
| 7 | 1 | 5 | 3 | 6 | 8 | 2 | 2 | 5 | 3 | 0 | 8 | 4 | 9 | 4 | 8 | 8 | 6 |
| 8 | 0 | 4 | 7 | 6 | 1 | 0 | 3 | 0 | 0 | 7 | 6 | 8 | 8 | 7 | 5 | 5 | 7 |
| 0 | 7 | 5 | 6 | 1 | 4 | 8 | 3 | 6 | 8 | 5 | 6 | 3 | 1 | 0 | 7 | 2 | 5 |
| 1 | 7 | 7 | 9 | 0 | 2 | 0 | 1 | 9 | 2 | 4 | 1 | 7 | 7 | 3 | 6 | 3 | 7 |
| 2 | 3 | 1 | 5 | 1 | 1 | 5 | 4 | 4 | 8 | 3 | 0 | 7 | 8 | 0 | 5 | 9 | 7 |
| 0 | 4 | 4 | 0 | 5 | 1 | 7 | 1 | 4 | 2 | 8 | 6 | 4 | 5 | 3 | 6 | 3 | 0 |
| 3 | 2 | 1 | 2 | 1 | 6 | 4 | 6 | 8 | 6 | 9 | 0 | 6 | 3 | 8 | 3 | 8 | 2 |
| 8 | 3 | 9 | 2 | 8 | 5 | 7 | 8 | 3 | 4 | 6 | 8 | 7 | 1 | 9 | 1 | 2 | 9 |
| 4 | 1 | 0 | 3 | 8 | 9 | 0 | 8 | 4 | 2 | 6 | 1 | 2 | 5 | 4 | 0 | 9 | 2 |
| $\mathbf{5}$ | 2 | 8 | 9 | 0 | 0 | 8 | 9 | 6 | 9 | 0 | 5 | 3 | 3 | 6 | 3 | 3 | 6 |
| 3 | 4 | 0 | 4 | 0 | 9 | 1 | 4 | 6 | 2 | 6 | 2 | 1 | 3 | 2 | 1 | 0 |  |
| 4 | 2 | 1 | 7 | 4 | 9 | 1 | 0 | 3 | 8 | 6 | 8 | 1 | 3 | 6 | 6 | 5 |  |
| 3 | $\mathbf{4}$ | 3 | 4 | 6 | 4 | 3 | 6 | 6 | 7 | 9 | 9 | 2 | 9 | 1 | 8 | 4 | 1 |
| 6 | 2 | 4 | 9 | 4 | 5 | 6 | 9 | 5 | 3 | 9 | 2 | 9 | 3 | 7 | 9 | 7 | 9 |
| 0 | 3 | 4 | 4 | 4 | $\mathbf{4}$ | 2 | 2 | 0 | 6 | 4 | 8 | 7 | 7 | 1 | 8 | 7 | 8 |
| 7 | 1 | 9 | 6 | 1 | 1 | 2 | 5 | 6 | 4 | 2 | 9 | 2 | 4 | 5 | 1 | 5 | 2 |
| 2 | 1 | 9 | 9 | 9 | 4 | 5 | 9 | 4 | 2 | 9 | 3 | 7 | 6 | 4 | 6 | 0 | 3 |
| 7 | 3 | 8 | 3 | 6 | 4 | 2 | 9 | 6 | 4 | 5 | 1 | 1 | 3 | 8 | 8 | 8 | 2 |

## Or graph data?



Source: KEGG PATHWAY Database

## What does Tukey say?

Exploratory data analysis is detective work--numerical detective work-or counting detective work--or graphical detective work.

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As all detective stories remind us, many of the circumstances surrounding a crime are accidental or misleading. Equally, many of the indications to be discerned in bodies of data are accidental or misleading. To accept all appearances as conclusive would be destructively foolish, either in crime detection or in data analysis. To fail to collect all appearances because some--or even most--are only accidents would, however, be gross misfeasance deserving (and often receiving) appropriate punishment.

Exploratory data analysis can never be the whole story, but nothing else can serve as the foundation stone--as the first step.

Tukey, Exploratory Data Analysis (1977) pp. 1-3

Confirmatory analysis: Given one pre-planned hypothesis, infer parameter values or test hypotheses, judicial in character, set a high bar for what we are willing to believe about the data.

- Probability model for the data specified before analysis takes place
- Given the probability model, test hypotheses or infer parameter values

Exploratory analysis: Collect everything that even seems to be true about the data, detective in character, "magical thinking". Includes:

- Check distributional assumptions
- Check for outliers
- Decide on variable transformations
- Decide on the form of the model: what variables to include

Exploratory analysis: Collect everything that even seems to be true about the data, detective in character, "magical thinking". Includes:

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BUT: Not limited to the work done before fitting a model! In the highest points example, we had an EDA-based advance that wasn't related to model fitting at all.

Tukey's EDA also emphasizes tools and best practices for the practice of data analysis, all pen-and-paper based.

## Example: Tallying

Standard method:
/ // /// //// HHK

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Standard method:
/ // /// //// HHK

Tukey's proposal:

| 4 | is | $\because$ |
| ---: | :--- | :--- |
| 8 | is | $\square$ |
| 10 | is | $\boxtimes$ |

Pen-and-paper methods primarily of historical interest.

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Philosophical descendants are the tidyverse packages in R.

What about this class?

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Two categories of topics: what to do and how to do it.

For what to do, organize by type of data:

- Univariate data
- Bivariate data
- Trivariate/Hypervariate data
- Categorical data
- Distance data
- Other topics according to interest

In addition:

- Dangers of EDA and how to avoid potential problems

In the how to do it bin, we will learn to work with

- R
- ggplot2
- tidyverse packages

How is this class different from others?

- Machine learning: We put less emphasis on supervised learning.
- Data mining: More emphasis on visualization.
- Applied statistics: Less emphasis on $p$-values and inference, more flexibility in the methods used.

Texts:

- Cleveland, Visualizing Data
- Wickham, ggplot2: Elegant Graphics for Data Analysis
- Wickham and Grolemund, R for Data Science
- Other notes posted to the class website and canvas as necessary

Assessment:

- Homeworks (30\%).
- Mini project (20\%).
- Mini presentation (10\%).
- Final project ( $40 \%$ ).

How to succeed:

- Practice!
- Follow along with the code examples, actually type in the commands instead of copying and pasting.
- Start early on assignments and projects.
- Presentation matters - make your documents look nice enough that you would be happy to show them to potential employers as examples of your work.

For this week:

- Start thinking about a dataset to use for the mini presentation or the final project (can be the same for both).
- If you haven't installed R or RStudio yet, do it as soon as possible.
- I will post a sign-up sheet for the mini presentations this Sunday.

We will be exploring numbers. We need to handle them easily and look at them effectively. Techniques for handling and looking - whether graphical, arithmetic, or intermediate - will be important.

Tukey, Exploratory Data Analysis (1977)

